

Hamming's problem

- h is an “Ordered Set”
- $1 \in h$
- $x \in h \Rightarrow 2^*x \in h, 3^*x \in h, 5^*x \in h.$
- generate all elements of $h < \text{limit}$

Let's solve it

1. Write a test
2. make the test run green
3. clean up the code
 - remove any duplication
4. repeat until done

CS410/510 Advanced Programming

Lecture 7:

Regular Expressions in Smalltalk

Just Like Haskell

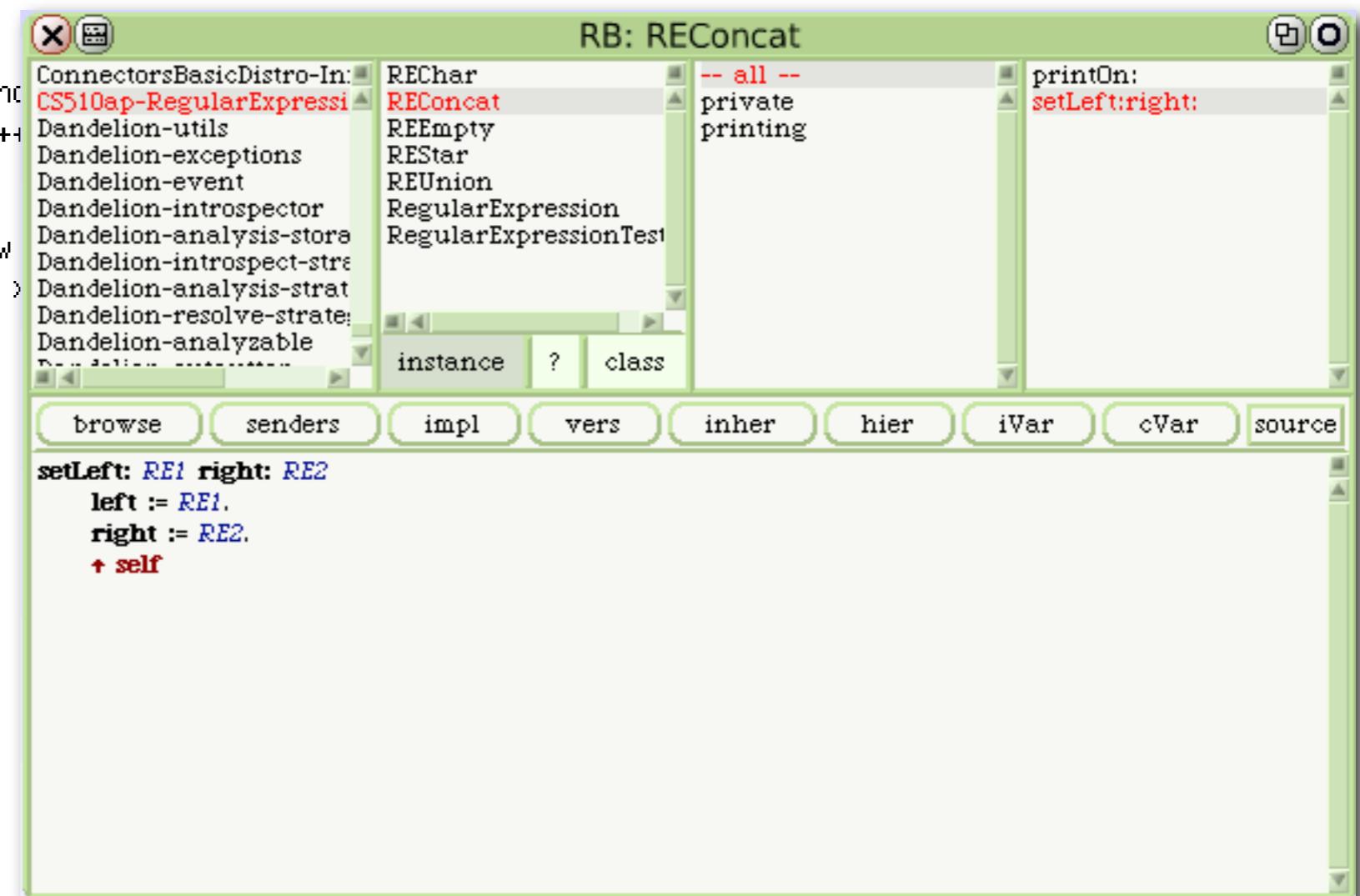
```
data RE
  = Empty
  | Union RE RE
  | Concat RE RE
  | Star RE
  | C Char

instance Show RE where
  show Empty = "#"
  show (C x) = [x]
  show (Union x y) = "("++showU x++"++"++showU y++)"
    where showU (Union x y) = show x++"++"++showU y
          showU x = show x
  show (Concat x y) = show x++show y
  show (Star (x@(Concat _ _))) = "("++show x++")*"
  show (Star (x@(Union _ _))) = "("++show x++")*"
  show (Star x) = show x++"*"
```

Just Like Haskell

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data RE
  = Empty
  | Union RE RE
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instance Show RE where
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```



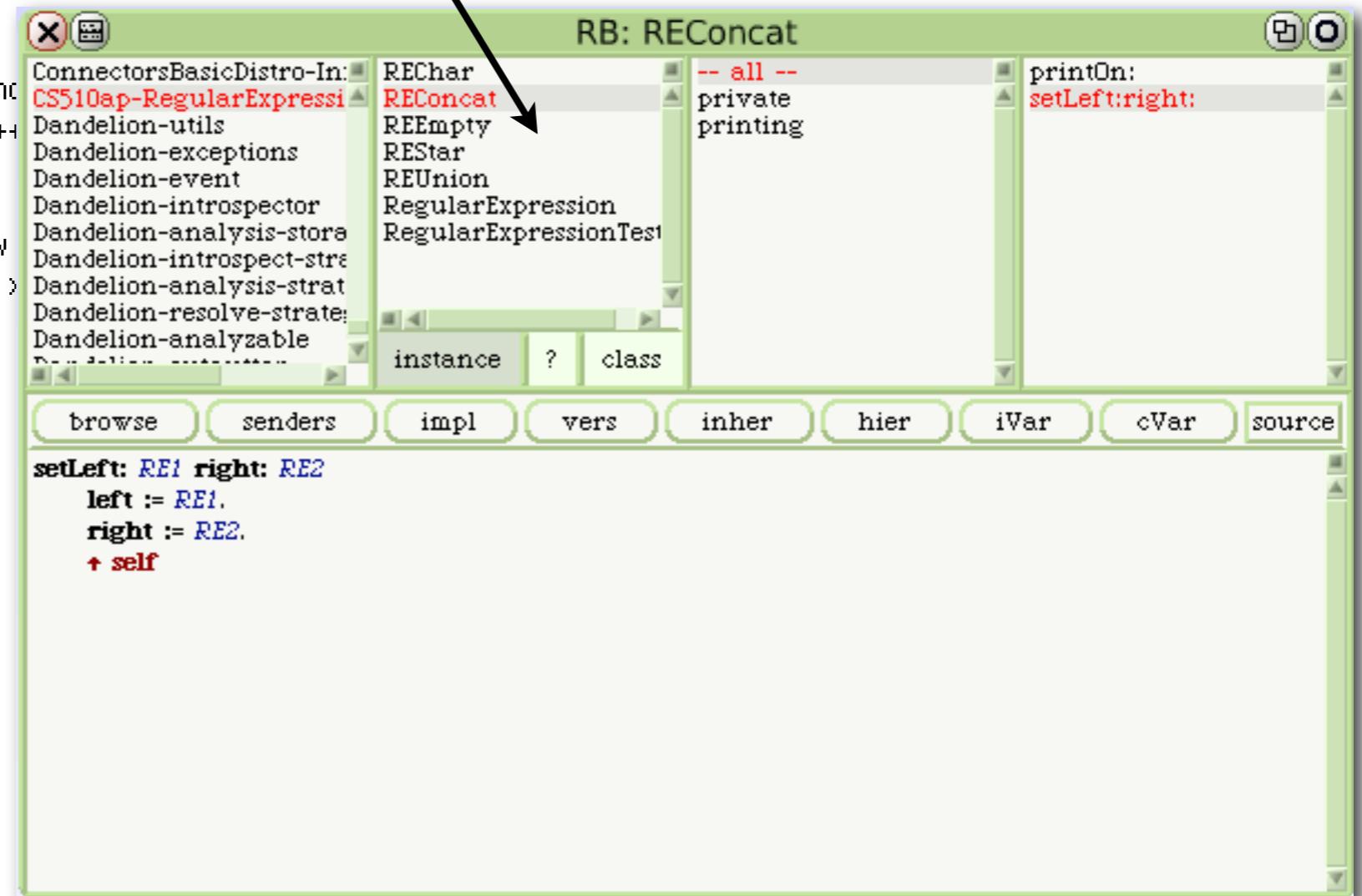
Just Like Haskell

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```

One subclass for each alternative representation



Write Tests

The screenshot shows the Smalltalk Inspector window titled "RB: RegularExpressionTests". The left pane displays the class hierarchy with "RegularExpressionTests" highlighted. The right pane shows the source code for the "setUp" method. The code initializes various regular expression objects:

```
super setUp.  
epsilon := REEmpty.  
a := REChar with: $a.  
b := REChar with: $b.  
aOrb := REUnion with: a with: b.  
ab := REConcat with: a with: b.  
abStar := RESTar with: ab
```

Write Tests

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abStar := RESTar with: ab
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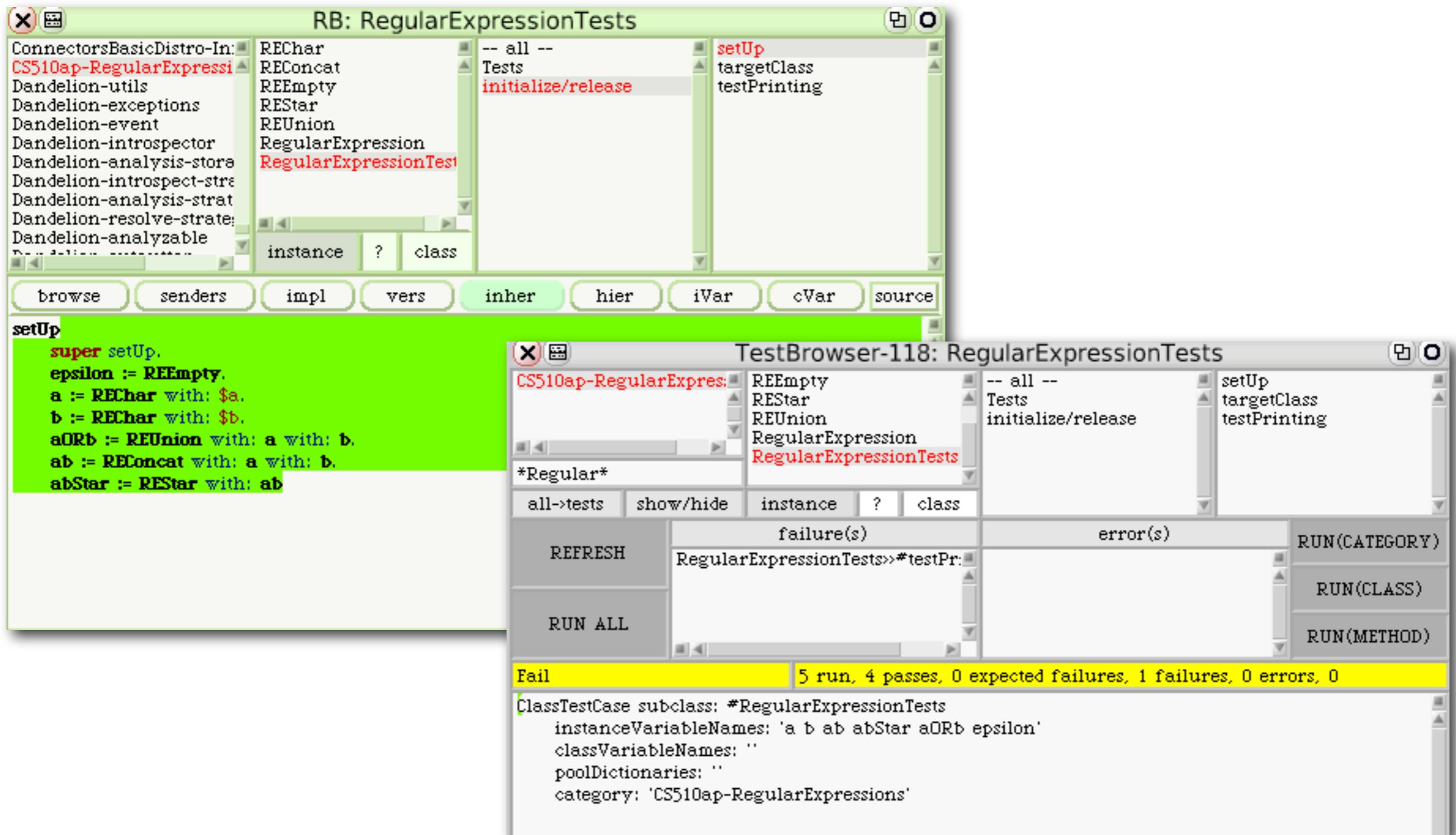
1. Run tests
2. get *message not understood*
3. define method
4. repeat from 1
- ...
19. get real failure

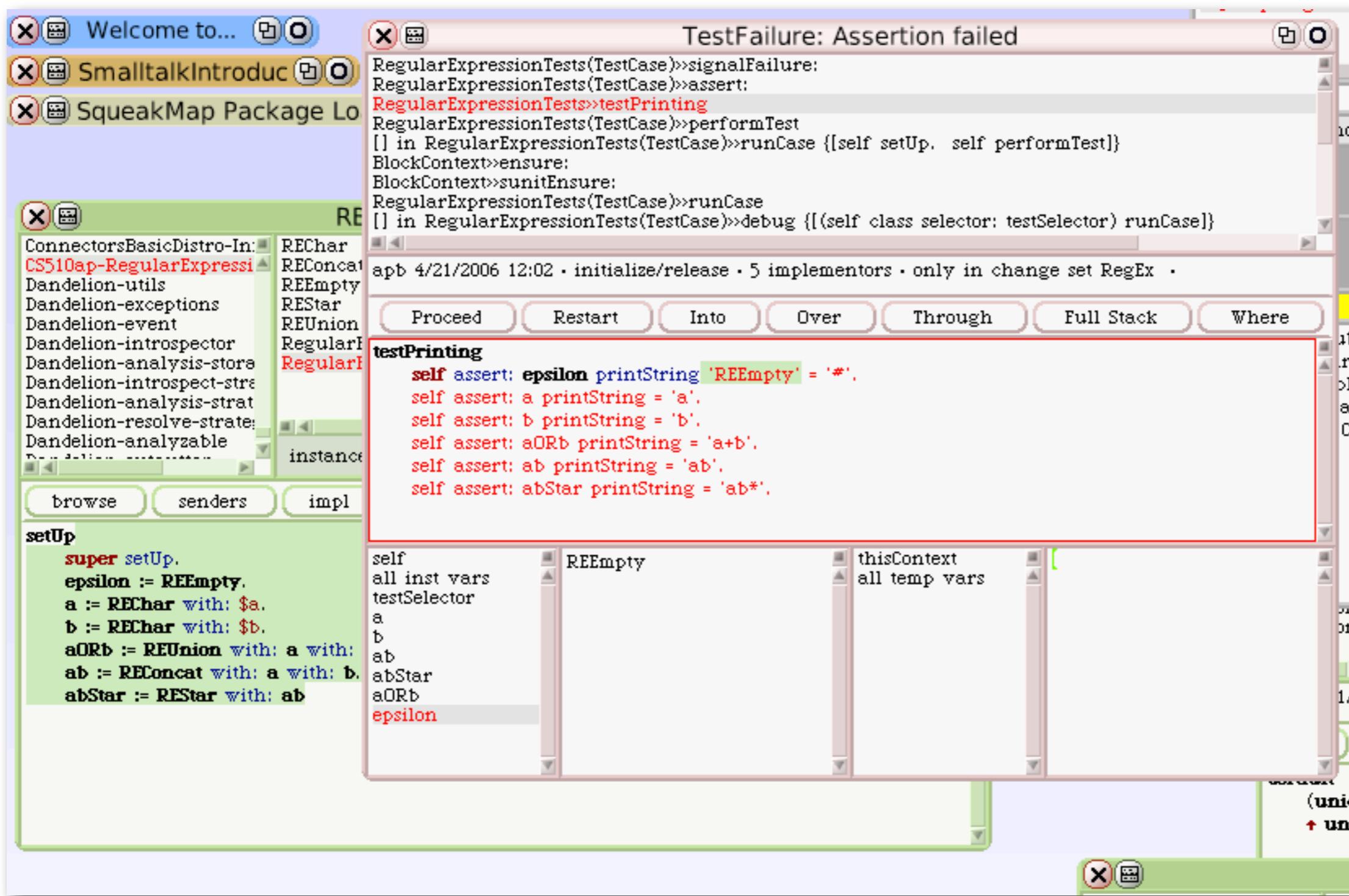
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Write Tests





What's the problem?

I need an instance, not the class

- But there need be only one instance of REEmpty
- Enter: the Singleton pattern.
 - make a class instance-variable called uniqueInstance
 - make a class-side method named default

```
default
```

```
uniqueInstance ifNil: [uniqueInstance := self basicNew].  
^ uniqueInstance
```

- override new to be an error

What do we have so far?

The screenshot shows the Dandelion application interface. On the left is a sidebar window titled "Dandelion" with the following content:

- [Overview](#)
- [Whole Index](#)
- [All Classes](#)
- [All Categories](#)

Below these are two scroll bars. The main content area has a title "Dandelion" and contains two sections:

- All Categories**
 - [CS510ap-RegularExpressions](#)
- All Globals**
 - [ActiveEvent](#)
 - [ActiveHand](#)
 - [CustomEventsRegistry](#)
 - [Display](#)
 - [ImageImports](#)
 - [Processor](#)
 - [ScheduledControllers](#)
 - [ScriptingSystem](#)
 - [Sensor](#)
 - [Smalltalk](#)
 - [SourceFiles](#)
 - [SystemOrganization](#)
 - [TestConstants](#)
 - [Transcript](#)

At the bottom of the sidebar, there is a link [^top](#) and a note *- made by Dandelion*. The main content area also has scroll bars.

Convenience Operations

```
alpha = Union (C 'a')
            (Union (C 'b') (C 'c'))
digit = Union (C '0')
            (Union (C '1') (C '2'))
key = Union (string "if")
            (Union (string "then")
                  (string "else"))
punc = (C ',')
ident = Concat alpha
            (Star (Union alpha digit))
number = Concat digit (Star digit)
lexer = Union ident (Union number (Union key punc))

val re1 = Concat(Union (C '+')(Union (C '-')Empty))
                (Concat (C 'D')(Star (C 'D'))))

string :: String -> RE
string [] = Empty
string [c] = C c
string (c:cs) = Concat (C c) (string cs)
```

- Write tests:

self assert: \$a asRE printString = 'a'

self assert: (a + b) printString = 'a+b'

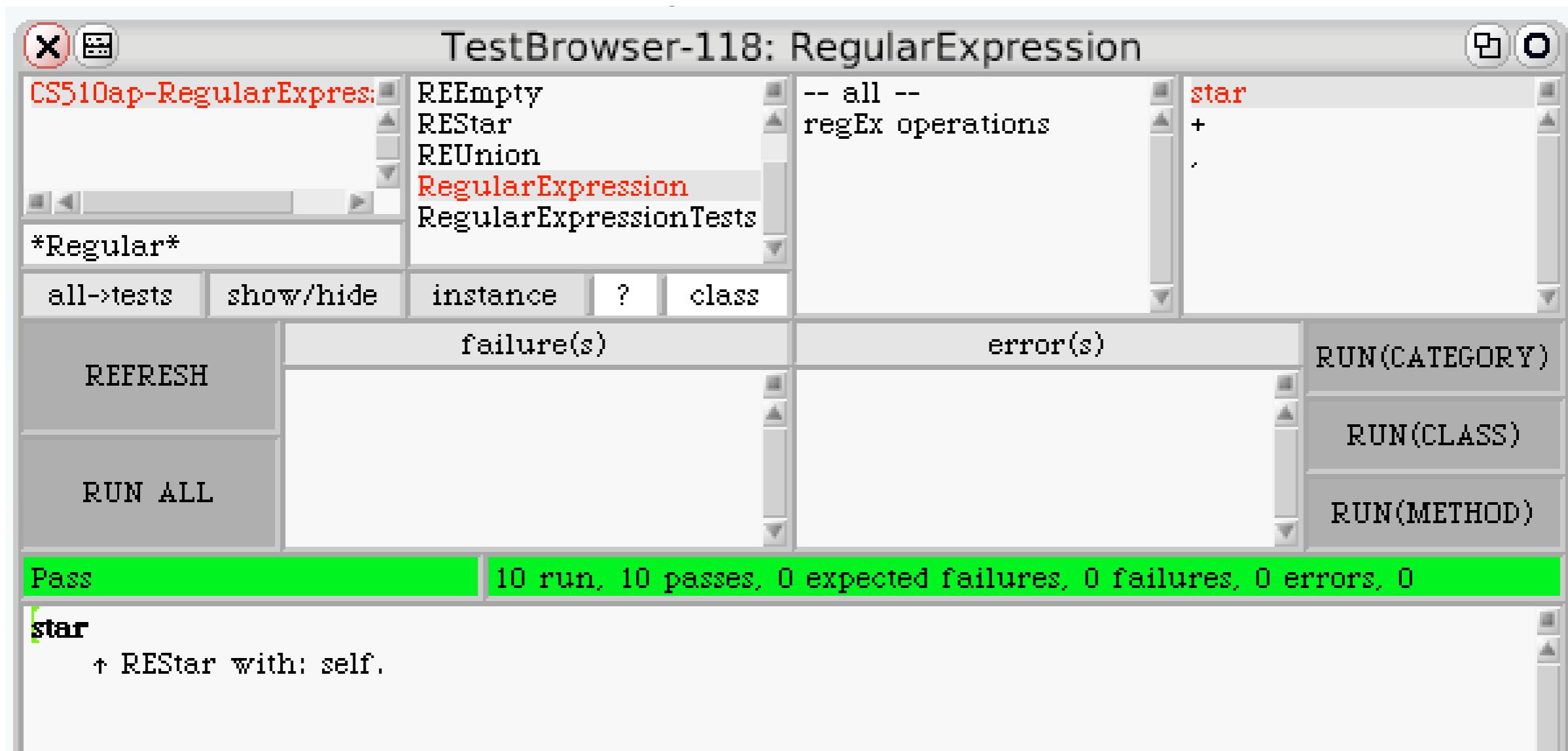
- Why compare *printStrings*?

Where do the operation methods go?

- In the abstract superclass `RegularExpression`
 - so that they work for all the subclasses

Where do the operation methods go?

- In the abstract superclass `RegularExpression`



Refactor tests to remove duplication

testPrinting

```
self assert: epsilon printsAs: '#'.
self assert: a printsAs: 'a'.
self assert: b printsAs: 'b'.
self assert: aORb printsAs: 'a+b'.
self assert: ab printsAs: 'ab'.
self assert: abStar printsAs: 'ab*'.
```

assert: anExpression printsAs: aprintString

```
self assert: anExpression printString = aprintString
```

which brings us to...

The screenshot shows a software interface for the Dandelion system. On the left, there's a sidebar with links to 'Dandelion Overview' and 'Whole Index', followed by 'All Classes' and 'All Categories'. Below these are two scrollable lists: 'All Classes' containing items like REChar, REConcat, REEmpty, REStar, REUnion, RegularExpression, and another RegularExpression entry; and 'All Globals' containing ActiveEvent, ActiveHand, CustomEventsRegistry, Display, ImageImports, Processor, ScheduledControllers, ScriptingSystem, Sensor, Smalltalk, SourceFiles, and SystemOrganization. The main title 'Dandelion' is centered at the top of the main content area.

Dandelion

All Categories

[CS510ap-RegularExpressions](#)

All Globals

[ActiveEvent](#)
[ActiveHand](#)
[CustomEventsRegistry](#)
[Display](#)
[ImageImports](#)
[Processor](#)
[ScheduledControllers](#)
[ScriptingSystem](#)
[Sensor](#)
[Smalltalk](#)
[SourceFiles](#)
[SystemOrganization](#)

meaning1: sets of strings

- Code very similar to Tim's Haskell version
- Only tricky part is star
 - Haskell version:

```
meaning1 (Star r) = norm(zero ++ one ++ two ++ three)
where zero = []
      one = meaning1 r
      two = [x++y | x <- one, y <- one]
      three = [x++y | x <- one, y <- two]
```

Smalltalk

REStar

meaning1

```
| zero one two three |
zero := ''.
one := base meaning1.
two := self anyOf: one followedByAnyOf: one.
three := self anyOf: one followedByAnyOf: two.
+ (Set with: zero) addAll: one;
  addAll: two;
  addAll: three;
  yourself
```

RegularExpression

anyOf: ml followedByAnyOf: mr

```
| result |
result := Set new.
ml do: [:l | mr do: [:r | result add: l , r]].
+result
```

- Complicated enough to need a helper method
- Is there a simpler way to calculate * ?

Cross tests

```
Pass 17 run, 17 passes, 0 expected failures, 0 failures, 0 errors
[testMeaning1AgainstMeaning2
    self instanceVariableValues select: [ :each | each respondsTo: #meaning1 ] thenDo:
        [ :re | re meaning1 do: [ :str | self assert: (re meaning2: str) ] ]
```

- introspect on the instance variables of the test case
 - select those that respond to the `meaning1` message
 - check that for every string `str` in `re meaning1`
 - `re meaning2: str` is true

Now RE's pass the tests

The screenshot shows the Dandelion JavaDoc interface. On the left, there is a sidebar with links for Dandelion Overview and Whole Index, followed by All Classes and All Categories. Below these are two sections: All Classes (listing REChar, REConcat, REEmpty, REStar, REUnion, RegularExpres, and RegularExpres) and All Globals (listing ActiveEvent, ActiveHand, CustomEventsRegistry, Display, ImageImports, Processor, ScheduledControllers, ScriptingSystem, Sensor, Smalltalk, SourceFiles, SystemOrganization, TestConstants, and Transparency). The interface has scroll bars on the right side.

Dandelion

[All Categories](#)

[CS510ap-RegularExpressions](#)

All Globals

[ActiveEvent](#)
[ActiveHand](#)
[CustomEventsRegistry](#)
[Display](#)
[ImageImports](#)
[Processor](#)
[ScheduledControllers](#)
[ScriptingSystem](#)
[Sensor](#)
[Smalltalk](#)
[SourceFiles](#)
[SystemOrganization](#)
[TestConstants](#)
[Transparency](#)

Finite State Machines

FINITE AUTOMATA AND REGULAR GRAMMARS

3.1 THE FINITE AUTOMATON

In Chapter 2, we were introduced to a generating scheme—the grammar. Grammars are finite specifications for languages. In this chapter we shall see another method of finitely specifying infinite languages—the recognizer. We shall consider what is undoubtedly the simplest recognizer, called a finite automaton. The finite automaton (fa) cannot define all languages defined by grammars, but we shall show that the languages defined are exactly the type 3 languages. In later chapters, the reader will be introduced to recognizers for type 0, 1, and 2 languages. Here we shall define a finite automaton as a formal system, then give the physical meaning of the definition.

A *finite automaton* M over an alphabet Σ is a system $(K, \Sigma, \delta, q_0, F)$, where K is a finite, nonempty set of *states*, Σ is a finite *input alphabet*, δ is a mapping of $K \times \Sigma$ into K , q_0 in K is the *initial state*, and $F \subseteq K$ is the set of *final states*.

Our model in Fig. 3.1 represents a finite control which reads symbols from a linear input tape in a sequential manner from left to right. The set of states K consists of the states of the finite control. Initially, the finite control is in state q_0 and is scanning the leftmost symbol of a string of symbols in Σ which appear on the input tape. The interpretation of $\delta(a, a) = n$, for a

The code with NFSM

The screenshot shows the Dandelion IDE interface. The left pane contains a sidebar with links for 'Dandelion Overview' and 'Whole Index', followed by 'All Classes' and 'All Categories'. Below these are scroll bars and a list of classes under 'All Classes' starting with `FSMState`. The right pane has a title 'Dandelion' and a 'All Categories' section containing `CS510ap-RegularExpressions`. It also has an 'All Globals' section listing various global variables.

Dandelion

[Overview](#)
[Whole Index](#)

[All Classes](#)

All Categories

CS510

All Classes

- [FSMState](#)
- [FSMStateSet](#)
- [NFSM](#)
- [NFSMTests](#)
- [REChar](#)
- [REConcat](#)
- [REEmpty](#)
- [REStar](#)
- [REUnion](#)
- [RegularExpression](#)
- [RegularExpression](#)

[^top](#)

- made by Dandelion

=

Dandelion

All Categories

[CS510ap-RegularExpressions](#)

All Globals

[ActiveEvent](#)
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[SourceFiles](#)
[SystemOrganization](#)
[TestConstants](#)
[Transcript](#)
[Undeclared](#)